

# Solving Quadratics with the Quadratic Formula

## The Quadratic Formula and the Discriminant

**Quadratic Formula** The Quadratic Formula can be used to solve *any* quadratic equation once it is written in the form  $ax^2 + bx + c = 0$ .

<b>Quadratic Formula</b>	The solutions of $ax^2 + bx + c = 0$ , with $a \neq 0$ , are given by $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ .
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**Example** Solve  $x^2 - 5x = 14$  by using the Quadratic Formula.

Rewrite the equation as  $x^2 - 5x - 14 = 0$ .

$$\begin{aligned}x &= \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} && \text{Quadratic Formula} \\&= \frac{-(-5) \pm \sqrt{(-5)^2 - 4(1)(-14)}}{2(1)} && \text{Replace } a \text{ with } 1, b \text{ with } -5, \text{ and } c \text{ with } -14. \\&= \frac{5 \pm \sqrt{81}}{2} && \text{Simplify.} \\&= \frac{5 \pm 9}{2} \\&= 7 \text{ or } -2\end{aligned}$$

The solutions are  $-2$  and  $7$ .

## Roots and the Discriminant

<b>Discriminant</b>	The expression under the radical sign, $b^2 - 4ac$ , in the Quadratic Formula is called the <b>discriminant</b> .
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## Roots of a Quadratic Equation

Discriminant	Type and Number of Roots
$b^2 - 4ac > 0$ and a perfect square	2 rational roots
$b^2 - 4ac > 0$ , but not a perfect square	2 irrational roots
$b^2 - 4ac = 0$	1 rational root
$b^2 - 4ac < 0$	2 complex roots

**Example** Find the value of the discriminant for each equation. Then describe the number and types of roots for the equation.

a.  $2x^2 + 5x + 3$

The discriminant is

$$b^2 - 4ac = 5^2 - 4(2)(3) \text{ or } 1.$$

The discriminant is a perfect square, so the equation has 2 rational roots.

b.  $3x^2 - 2x + 5$

The discriminant is

$$b^2 - 4ac = (-2)^2 - 4(3)(5) \text{ or } -56.$$

The discriminant is negative, so the equation has 2 complex roots.

**6-5 Skills Practice*****The Quadratic Formula and the Discriminant***

Complete parts a–c for each quadratic equation.

a. Find the value of the discriminant.

b. Describe the number and type of roots.

c. Find the exact solutions by using the Quadratic Formula.

1.  $x^2 - 8x + 16 = 0$

2.  $x^2 - 11x - 26 = 0$

3.  $3x^2 - 2x = 0$

4.  $20x^2 + 7x - 3 = 0$

5.  $5x^2 - 6 = 0$

6.  $x^2 - 6 = 0$

7.  $x^2 + 8x + 13 = 0$

8.  $5x^2 - x - 1 = 0$

9.  $x^2 - 2x - 17 = 0$

10.  $x^2 + 49 = 0$

11.  $x^2 - x + 1 = 0$

12.  $2x^2 - 3x = -2$

Solve each equation by using the method of your choice. Find exact solutions.

13.  $x^2 = 64$

14.  $x^2 - 30 = 0$

15.  $x^2 - x = 30$

16.  $16x^2 - 24x - 27 = 0$

17.  $x^2 - 4x - 11 = 0$

18.  $x^2 - 8x - 17 = 0$

19.  $x^2 + 25 = 0$

20.  $3x^2 + 36 = 0$

21.  $2x^2 + 10x + 11 = 0$

22.  $2x^2 - 7x + 4 = 0$

23.  $8x^2 + 1 = 4x$

24.  $2x^2 + 2x + 3 = 0$

**25. PARACHUTING** Ignoring wind resistance, the distance  $d(t)$  in feet that a parachutist falls in  $t$  seconds can be estimated using the formula  $d(t) = 16t^2$ . If a parachutist jumps from an airplane and falls for 1100 feet before opening her parachute, how many seconds pass before she opens the parachute?